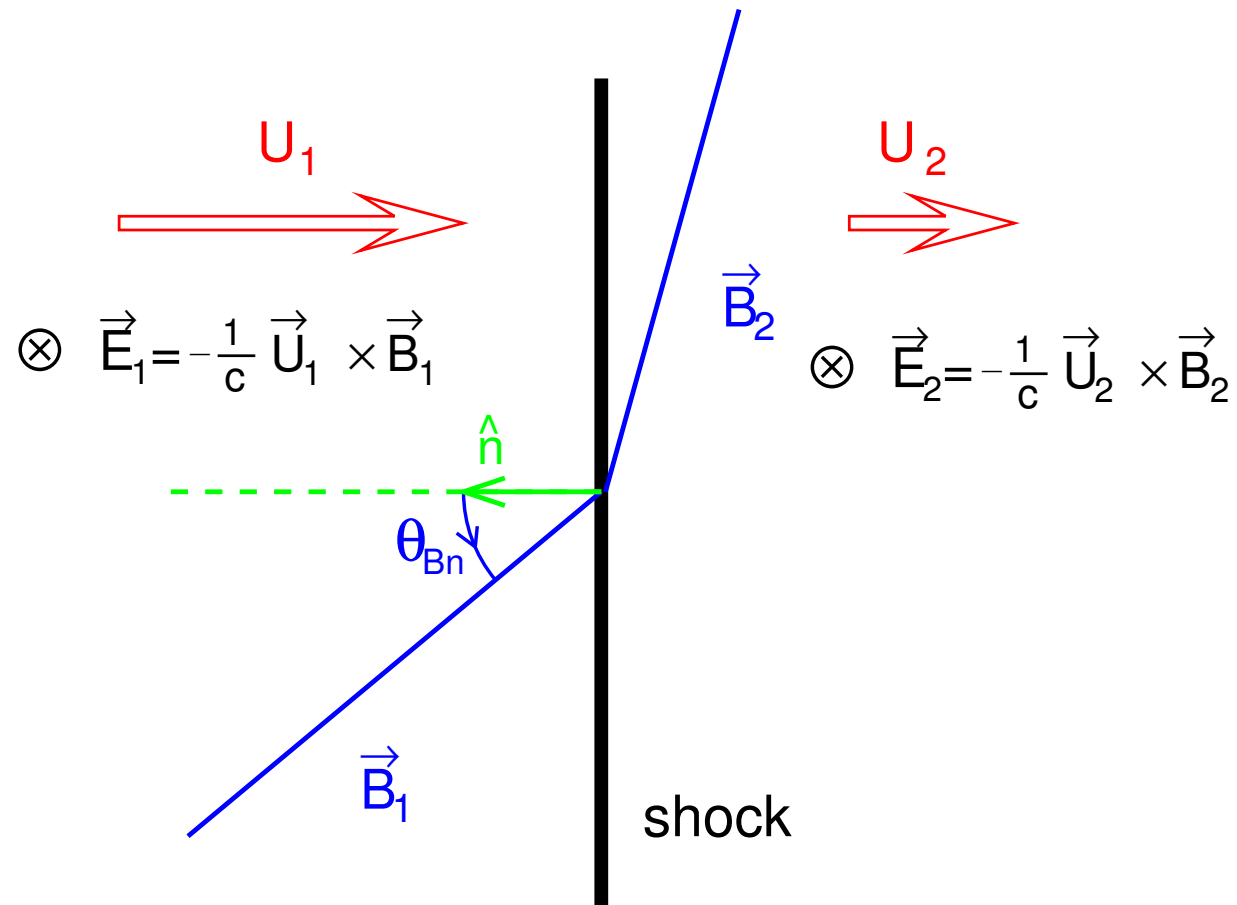


- **What is the Injection Energy Associated with Shock Acceleration?**
- **Does it depend on Shock-Normal Angle?**
- **What is the Acceleration Rate?**

# Simplified Shock Geometry



In order for particles to be accelerated by the shock – efficiently – they must remain near the shock.

In the **ABSENCE** of scattering, particles can remain ahead of the shock only if their speed,  $w$  is such that

$$w > V_1 \sec \theta_{Bn}$$

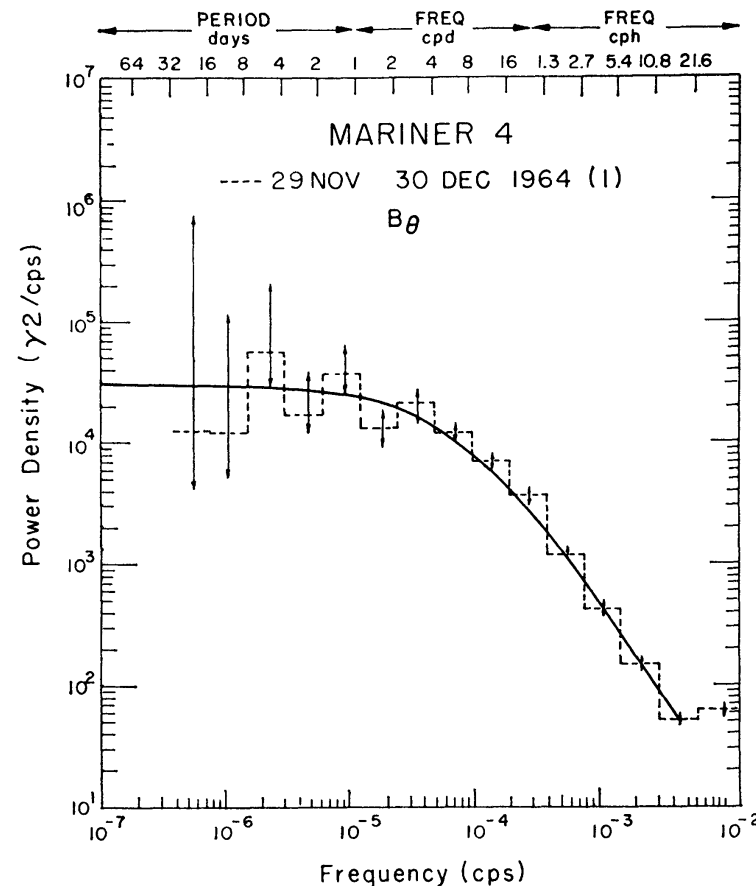
where  $V_1$  is the shock speed.

This implies a **STRONG** dependence on  $\theta_{Bn}$

**BUT IS THIS A GOOD APPROXIMATION?**

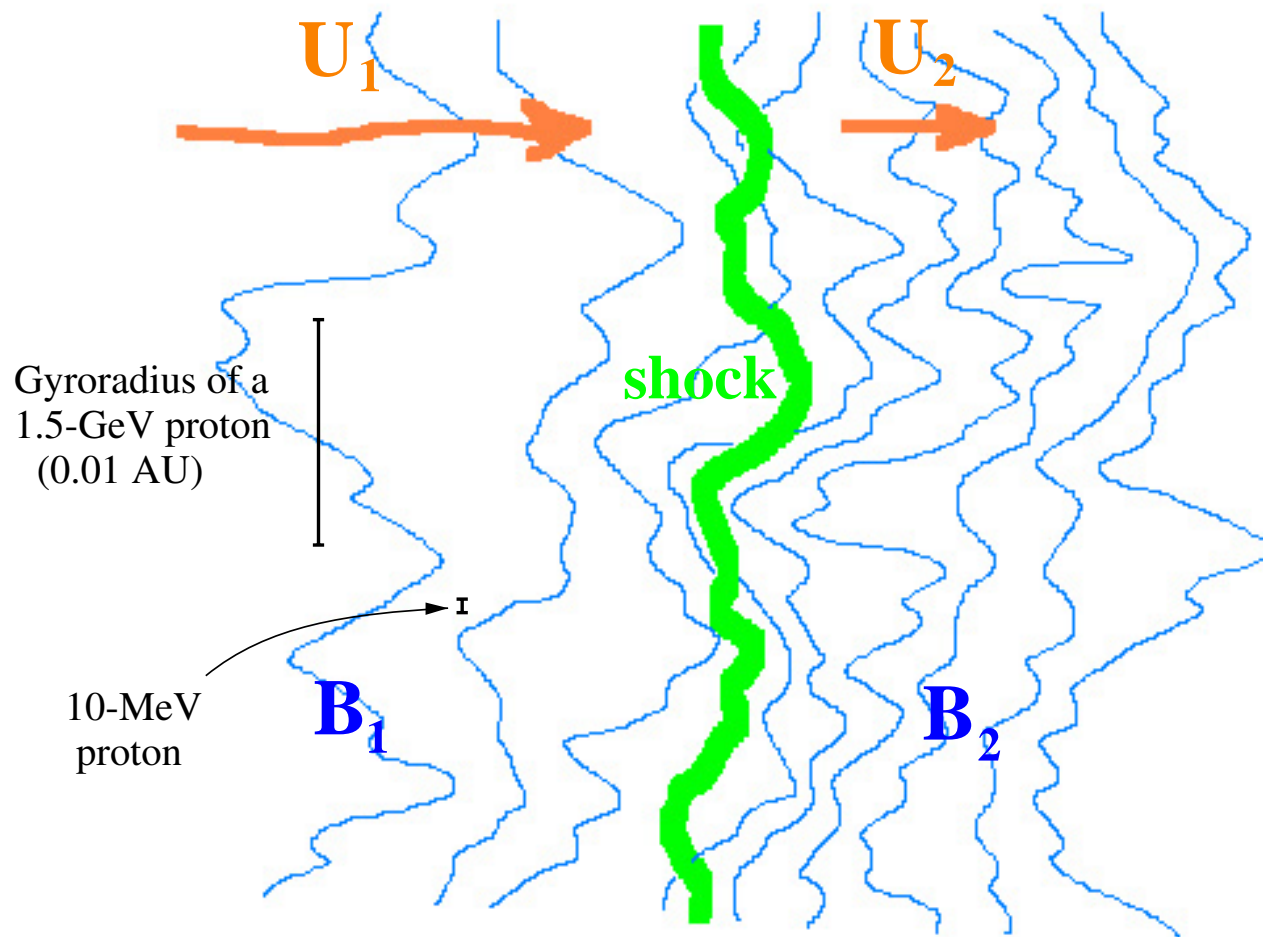
# AMBIENT FLUCTUATIONS

The coherence scale of the interplanetary magnetic field is about 0.01 AU (determined from power spectra)



Jokipii & Coleman, 1968

## A picture of the fields & flow near a shock at 1 AU



# The Limit of Diffusive Shock Acceleration

Diffusive shock-acceleration theory is valid if the anisotropy is small.  
The general expression is:

$$|\delta_i| = \frac{3U_1}{w} \left\{ 1 + \frac{\left(\frac{\kappa_A}{\kappa_{\parallel}}\right)^2 \sin^2 \theta_{Bn} + \left(1 - \frac{\kappa_{\perp}}{\kappa_{\parallel}}\right)^2 \sin^2 \theta_{Bn} \cos^2 \theta_{Bn}}{\left[\left(\frac{\kappa_{\perp}}{\kappa_{\parallel}}\right) \sin^2 \theta_{Bn} + \cos^2 \theta_{Bn}\right]^2} \right\}^{\frac{1}{2}}$$

$\ll 1 \quad \Rightarrow \quad$  Diffusive Shock Acceleration is applicable

# The Limit of Diffusive Shock Acceleration (cont.)

Case 1. Parallel shock ( $\theta_{Bn} \rightarrow 0$ )

$$\frac{3U_1}{w} \ll 1$$

Case 2. Perpendicular Shock ( $\theta_{Bn} \rightarrow 90$ )

$$\frac{3U_1}{w} \left[ 1 + \left( \frac{\kappa_A}{\kappa_{\perp}} \right)^2 \right]^{\frac{1}{2}} \ll 1$$



# The Limit of Diffusive Shock Acceleration (cont.)

Classical-scattering theory gives

$$\frac{\kappa_A}{\kappa_\perp} = \frac{\lambda_\parallel}{r_g} \gg 1 \quad (\text{for most astrophysical applications})$$

Thus, the classical-scattering theory predicts

$$w_{inj} \gg 3U_1(\lambda_\parallel/r_g)$$

# The Limit of Diffusive Shock Acceleration (cont.)

Classical-scattering theory gives

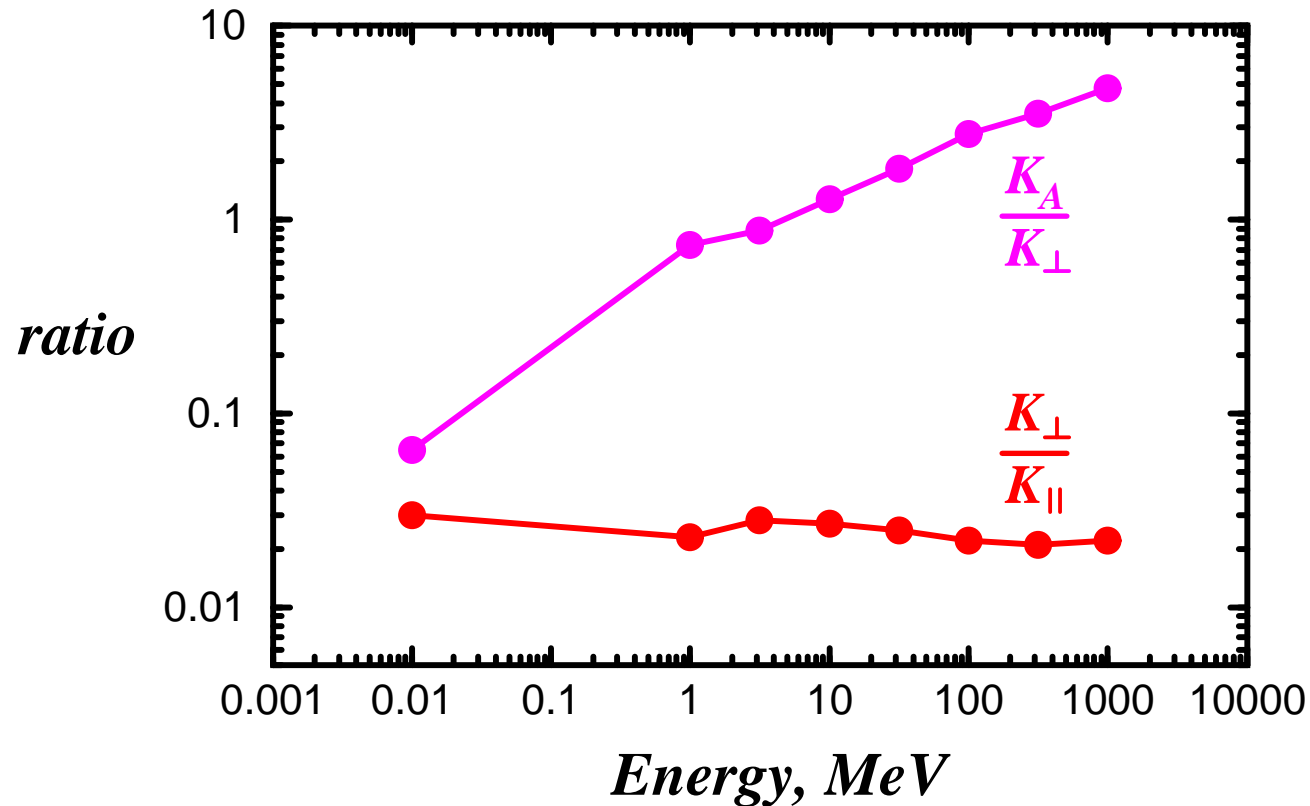
$$\frac{\kappa_A}{\kappa_\perp} = \frac{\lambda_\parallel}{r_g} \gg 1 \quad (\text{for most astrophysical applications})$$

Thus, the classical-scattering theory predicts

$$w_{inj} \gg 3U_1(\lambda_\parallel/r_g)$$

**HOWEVER**, classical-scattering theory is **NOT** a good approximation for perpendicular transport!

Test-particle simulations using synthesized magnetic turbulence  
(Giacalone and Jokipii, *ApJ*, 1999 + one extra point)



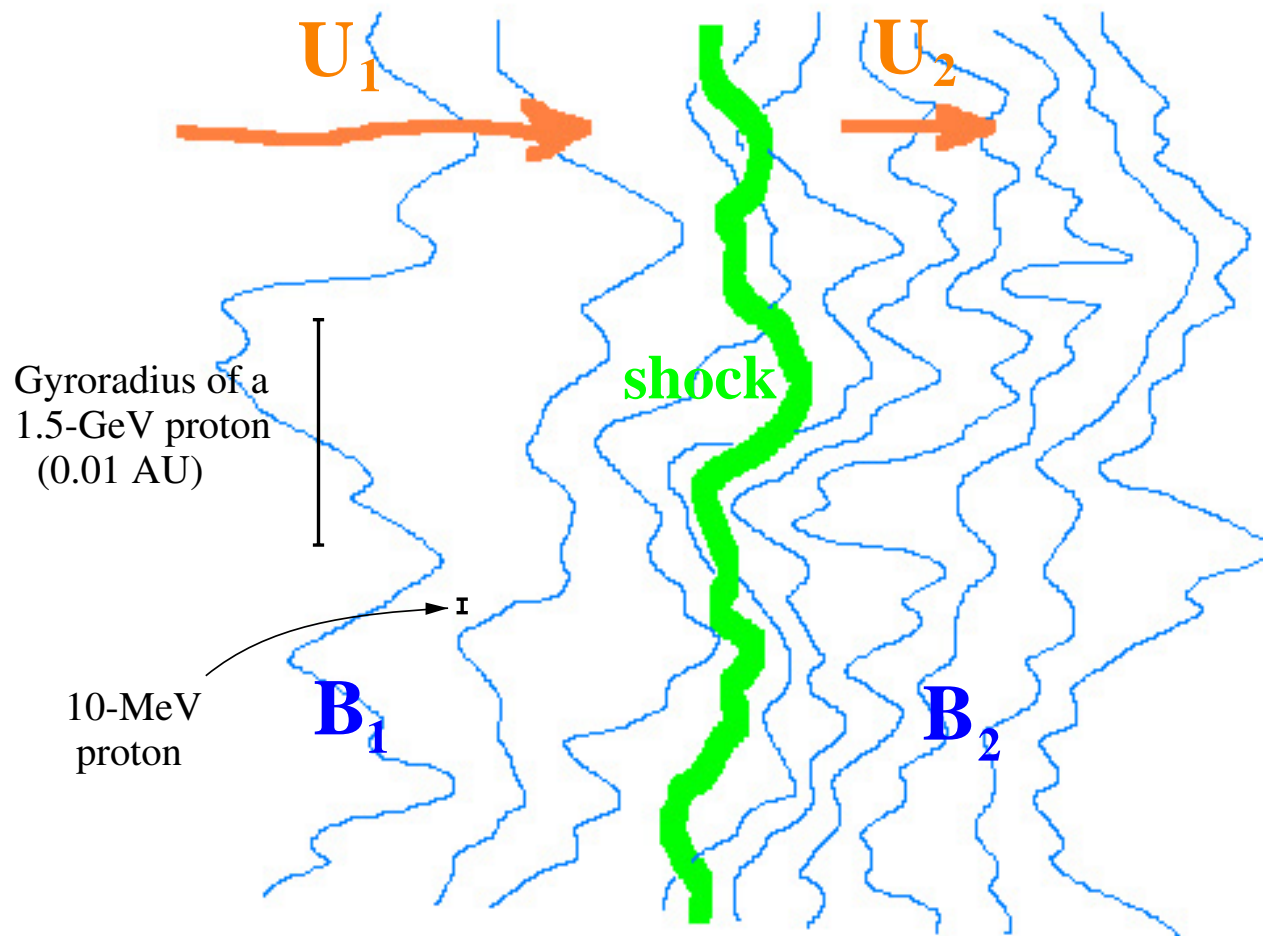
For a perpendicular shock, the injection velocity is given by

$$w_{inj} = 3U_1 \left[ 1 + \left( \frac{\kappa_A}{\kappa_{\perp}} \right)^2 \right]^{\frac{1}{2}}$$

$$\approx 3U_1$$

⇒ The SAME as for a parallel shock.

The Physics of self-excited waves is also affected by large-scale fluctuations – the time scale for wave growth and upstream scale length depend on the local geometry.



We wish to study particle acceleration and transport near a shock without invoking diffusive transport

In order to do this, we need to *synthesize* the turbulent fields.

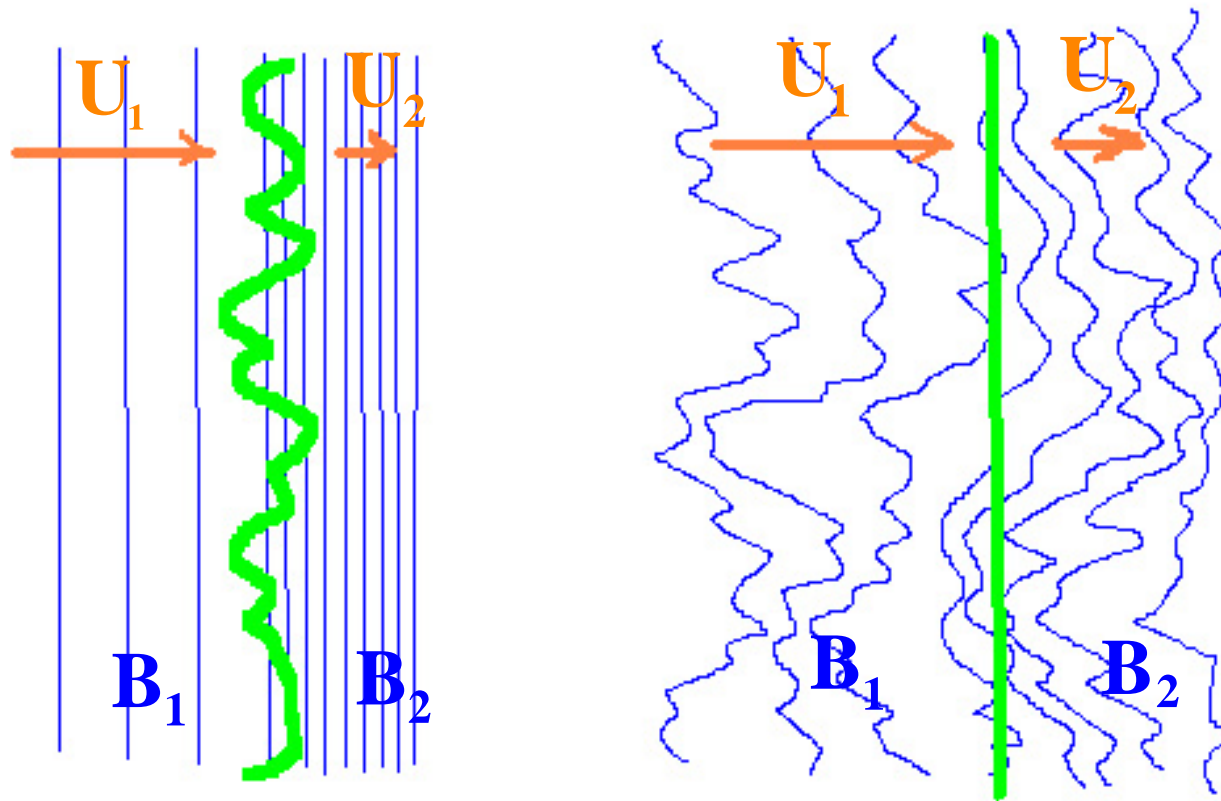
**There are two obvious ways to proceed:**

1. Turbulent ( “rippled” ) shock + magnetic field

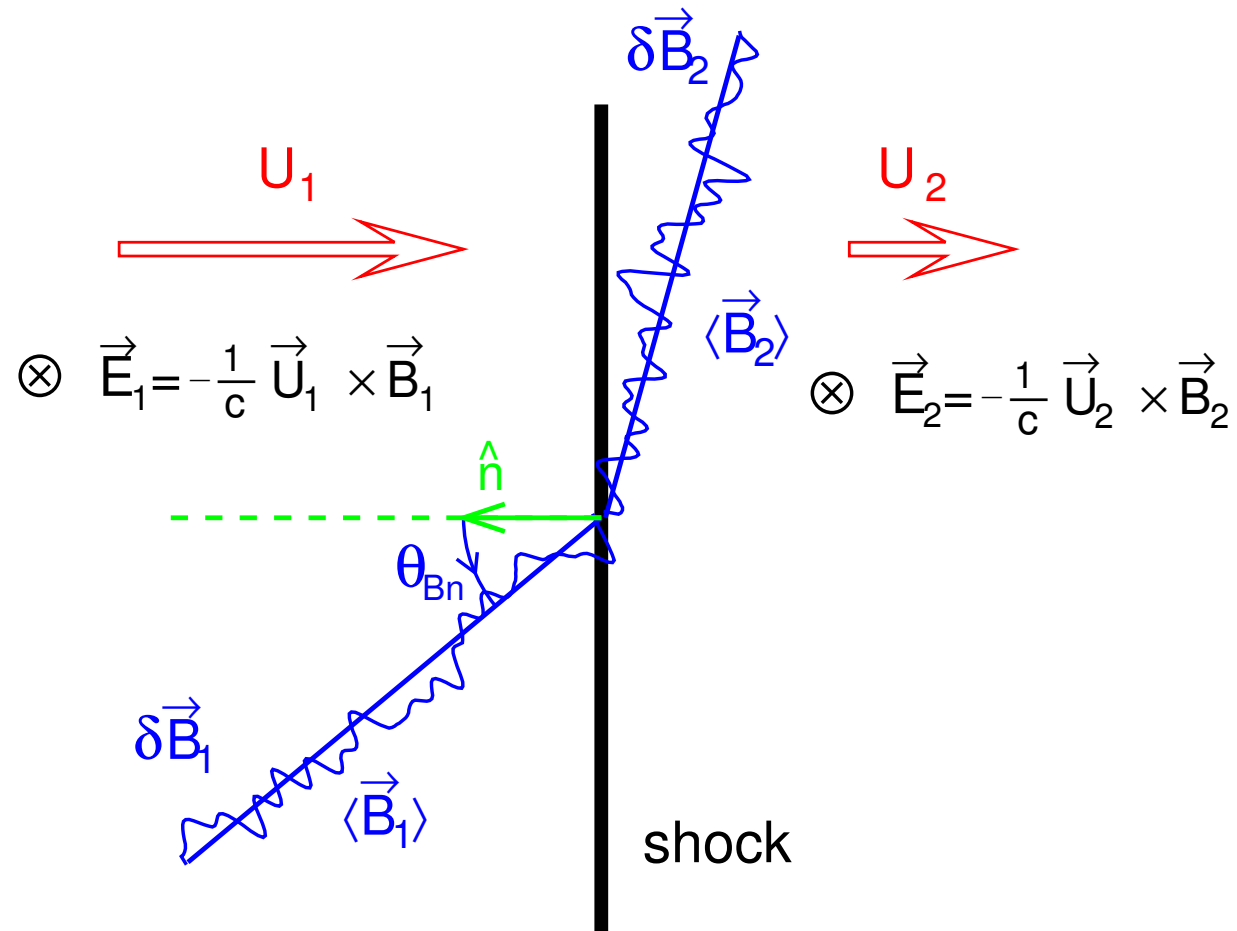
turns out to be difficult

2. Planar (or spherical) shock + turbulent magnetic field

# Modeling a shock moving through a turbulent medium

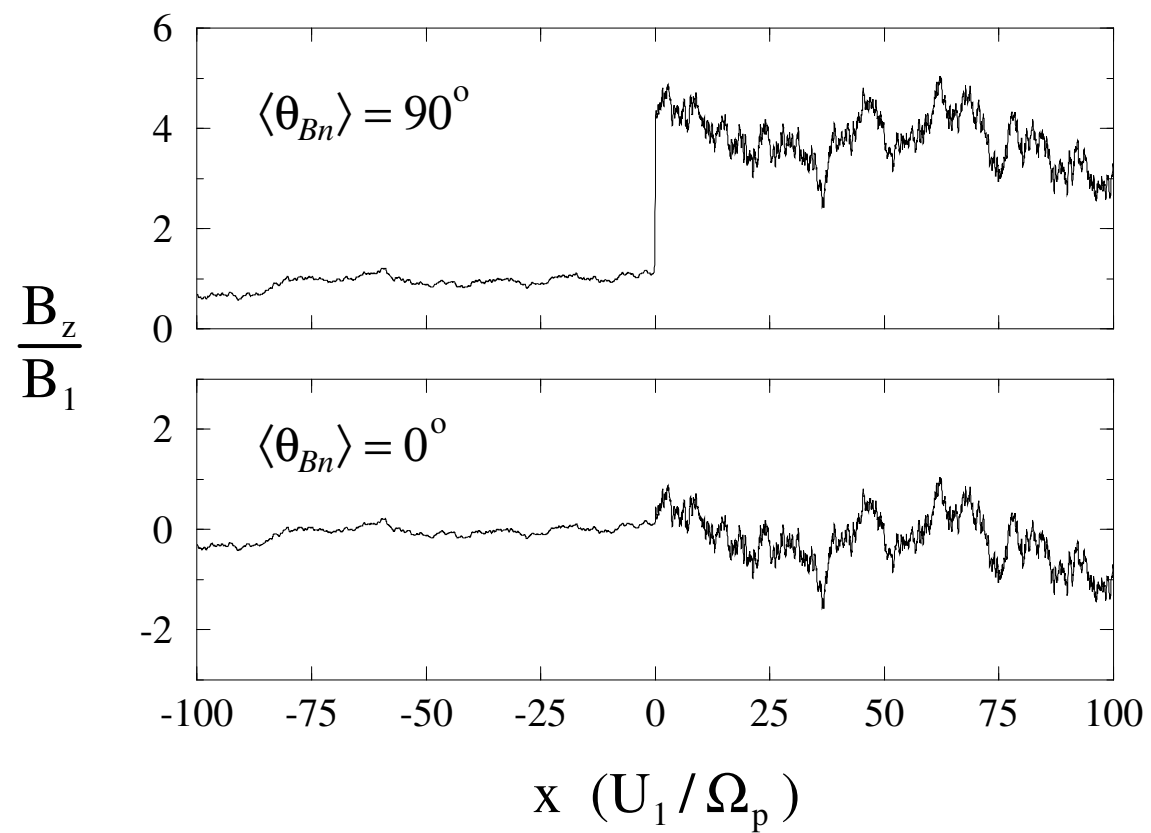


# Model Geometry

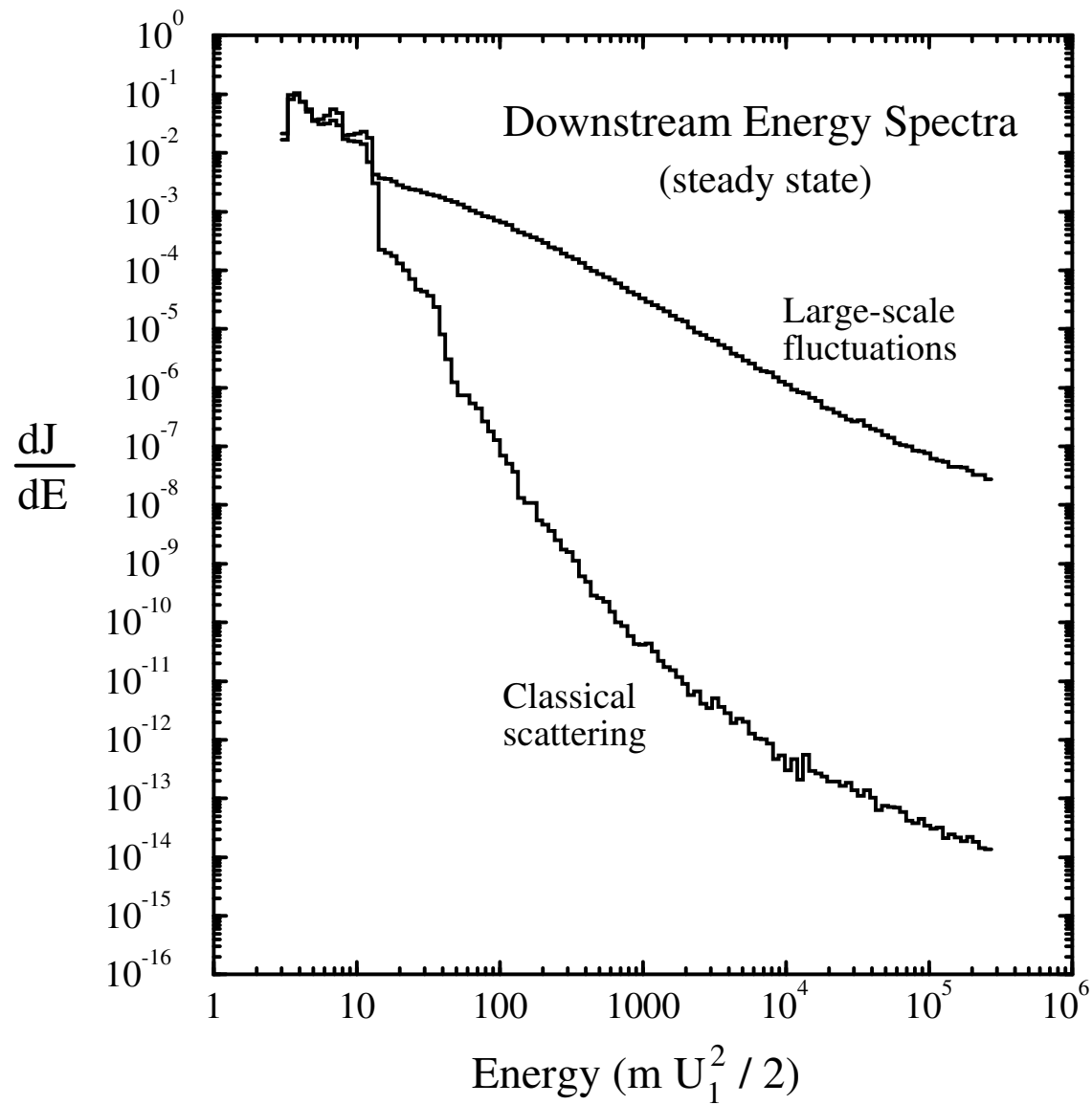




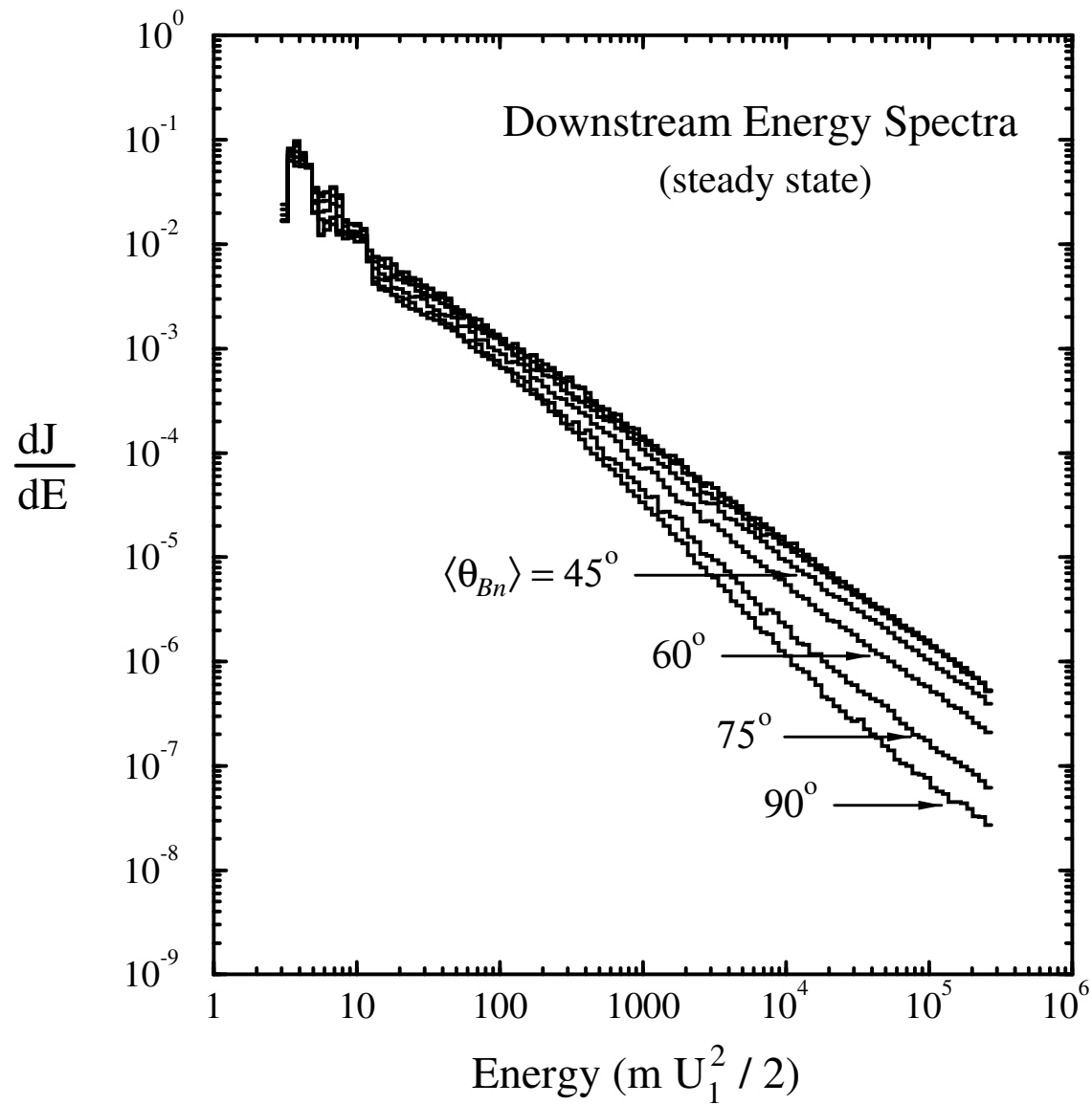
# Model Fields



# Model Results

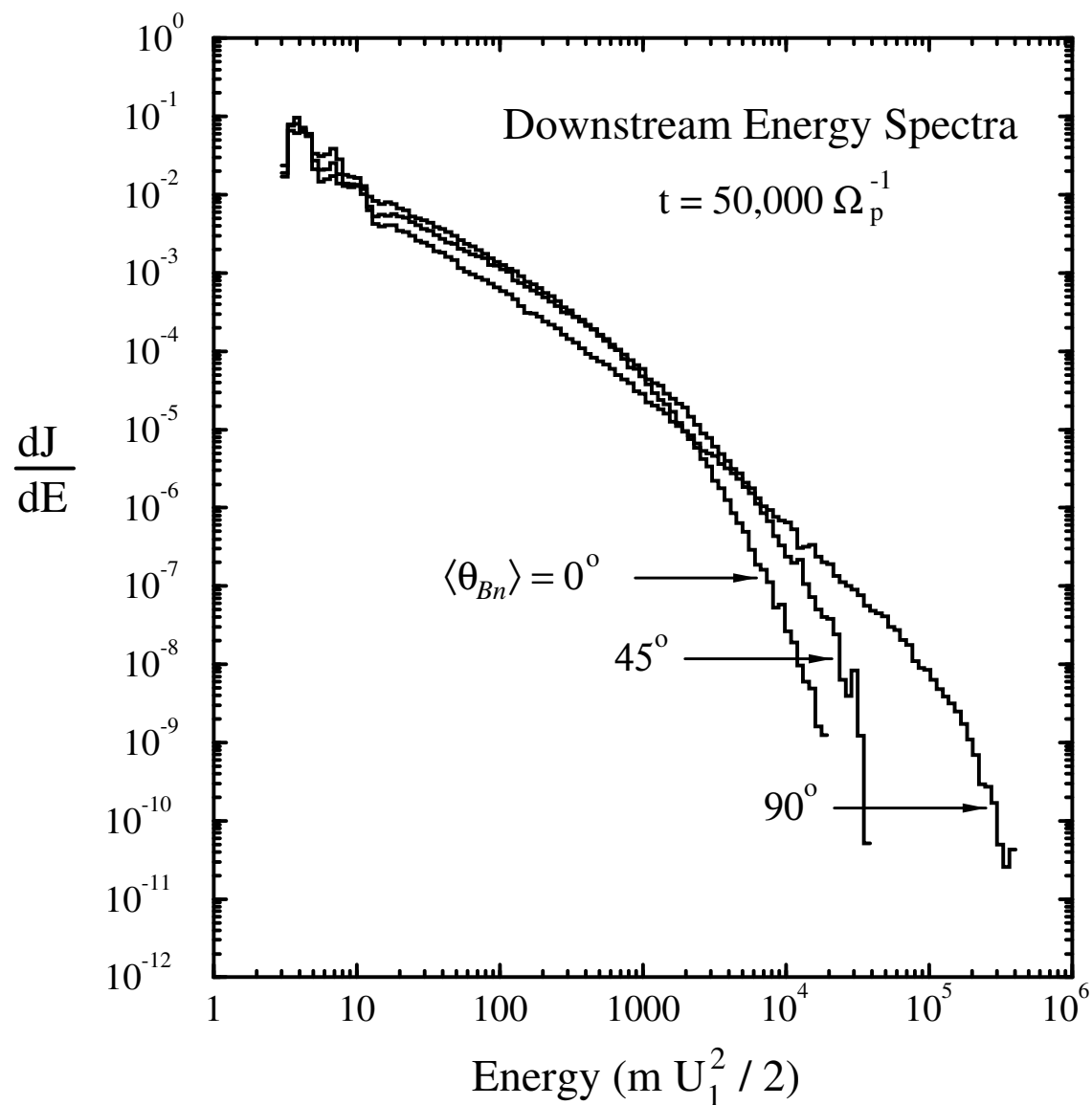


# Model Results

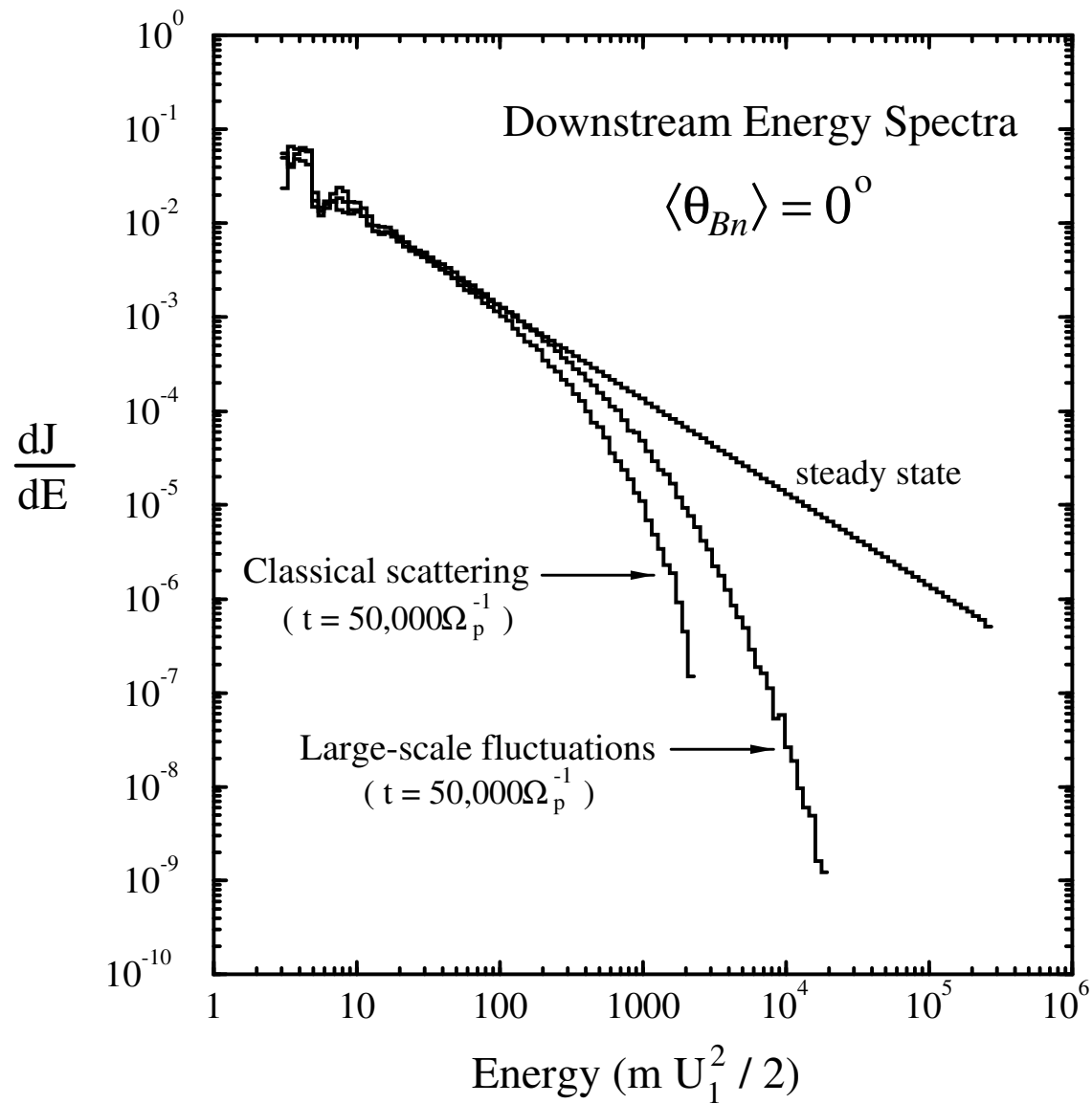


# Model Results

at  $10 R_{\odot}$ ,  $50,000 \Omega_p^{-1} \approx 6$  minutes



# Model Results

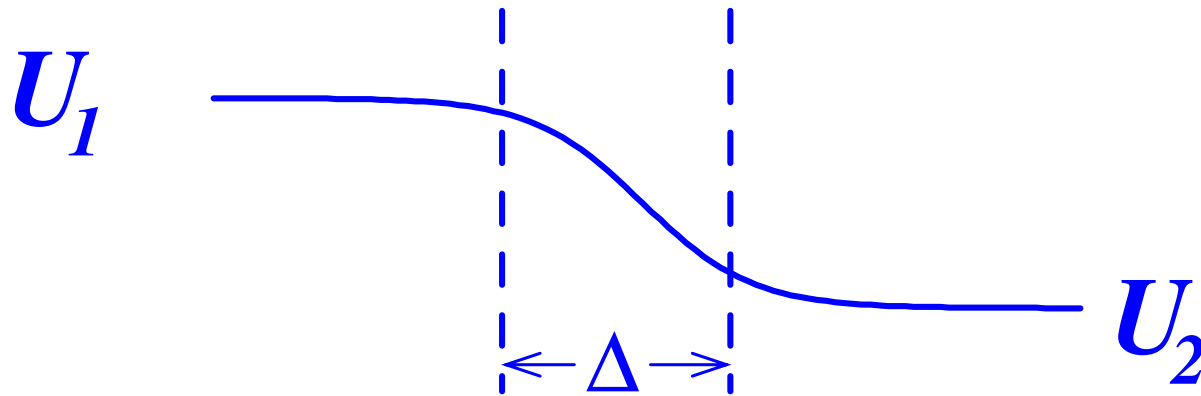


**CAN SHOCK ACCELERATION THEORY EXPLAIN THOSE  
EVENTS IN WHICH  $Fe/O$  INCREASES WITH ENERGY?**

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EVENTS IN WHICH  $FE/O$  INCREASES WITH ENERGY?**

**POSSIBLY YES – USING COMPRESSION ACCELERATION**

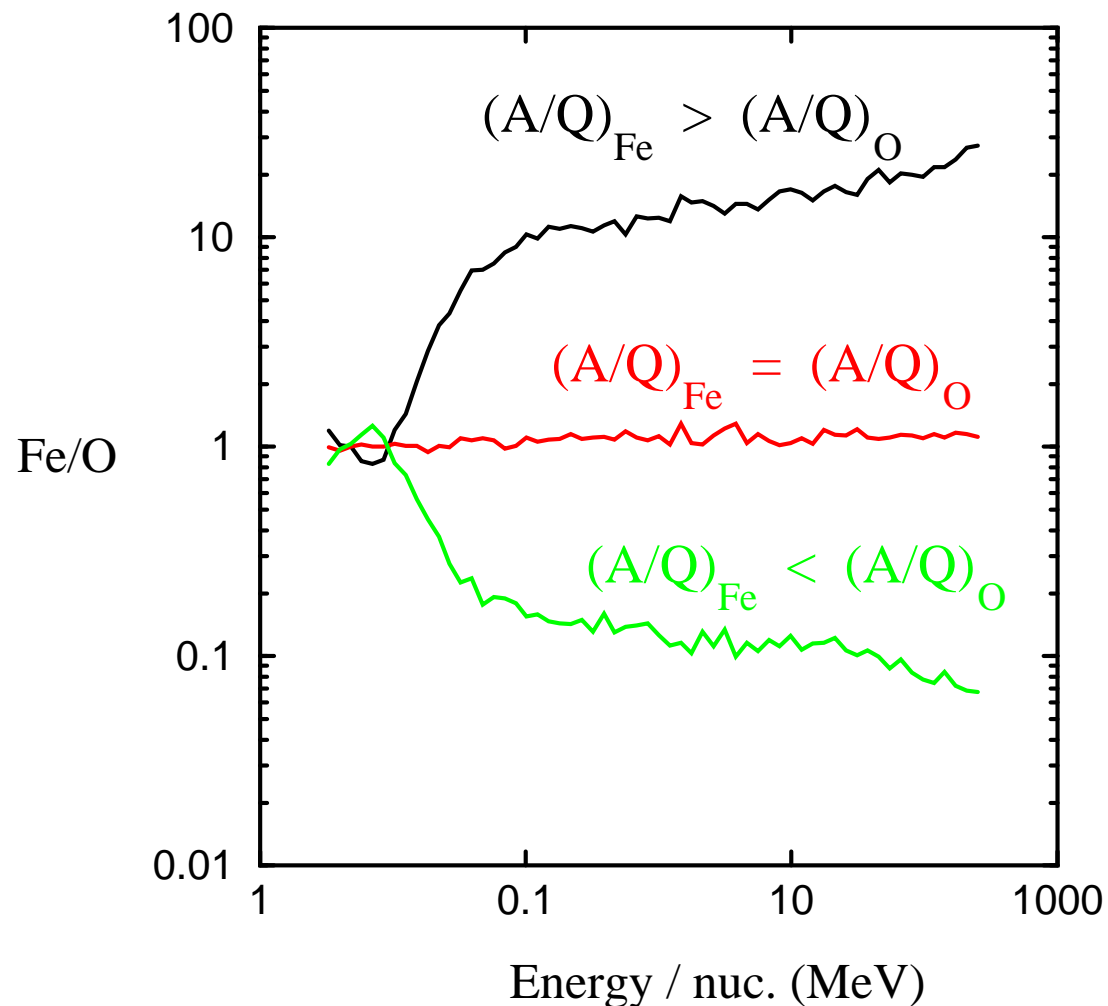
Consider a gradual plasma compression – NOT A SHOCK (e.g. CIRs at 1AU)



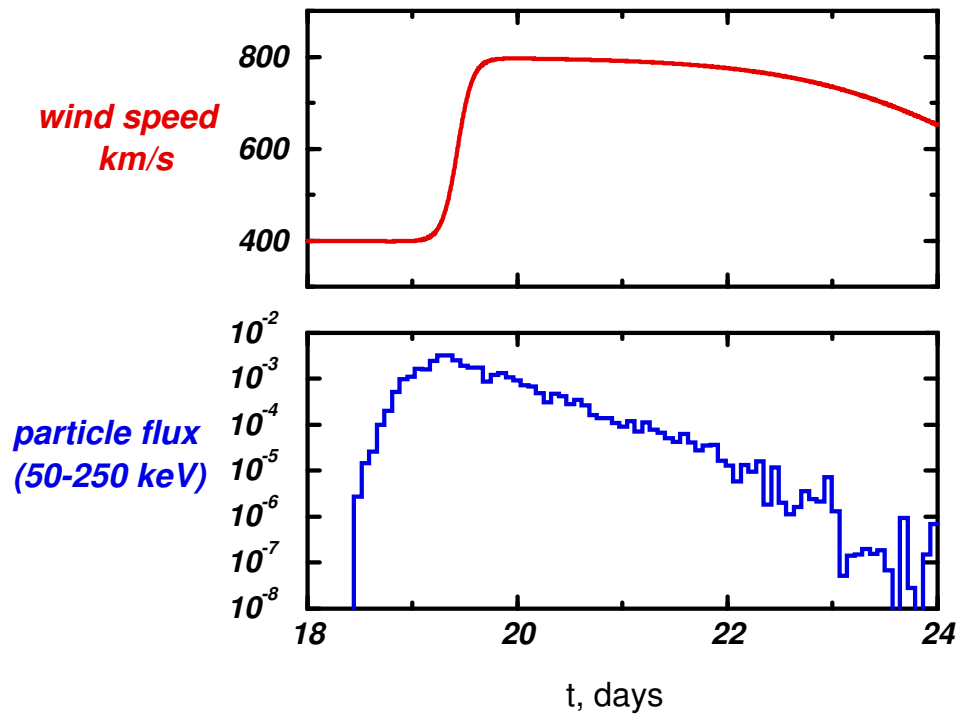
$$\Delta \gg c / \omega_i$$



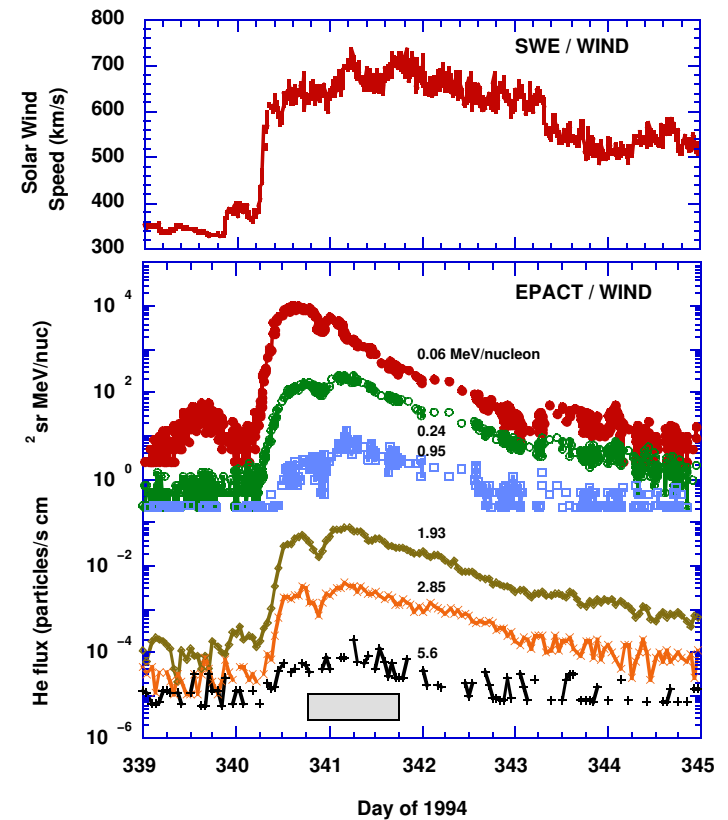
Acceleration of Fe and O at a gradual compression (three different charge states are considered)



## Simulations (Giacalone et al., 2002)



## Observations (Mason, 2000)



# Conclusions

1. For the case of strong IMF fluctuations ( $\Delta B^2 \sim B$ ) with a coherence scale of 0.01 AU, the injection velocity for shock acceleration is WEAKLY dependent on shock-normal angle.
2. Perpendicular shocks are more rapid accelerators of charged particles than parallel shocks – although the acceleration rate at a parallel shock is higher than expected from simple classical scattering theory.
3. Unusual enhancements of Fe/O may be due to acceleration at compression regions.